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**Multidimensional Data Object Searching Using Bit
Vector Indices**

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BACKGROUND

A number of strategies have been proposed for identifying and retrieving multimedia data objects stored in a database. At the heart of each of these strategies is a search problem, where a query point is compared to a set of multidimensional (MD) objects in the database. For example, a sample of a song having multiple characteristics (dimensions) may be compared to a number of songs stored in a database to find a song or songs having the same or similar characteristics. As a result of the search, either one or more matches are found, or no match exists in the set of objects in the database. These search problems are usually framed as some form of high dimensional search, where data and query points are mapped into the same high dimensional feature space. For a particular query point, a match is found by finding a data point in the feature space which is close enough to the query point to be considered a match. More specifically, these approximate matching problems are usually framed as epsilon distance queries using some L_p metric, such that the epsilon used is significantly less than the average interpoint distance.

Traditional query processing strategies for solving such problems (e.g. nearest neighbor, epsilon range searching), suffer poor performance due to intrinsic difficulties associated with high dimensionality. These traditional query processing strategies become even more problematic when different matching distances are used for different data points, which turns out to be a very important case for complex high dimensional searches, such as audio fingerprinting and the like. As a result, the most straightforward approach towards solving such problems, linear scan, has typically outperformed more sophisticated approaches. Unfortunately, while simple linear scanning typically achieves better performance

1 with respect to complex high dimensional searches than more complex query
2 processing strategies, linear scanning is a very time intensive process.

3 4 **SUMMARY**

5 Described herein are various systems and methods that facilitate rapid
6 searching of MD data objects in an MD feature space. In accordance with one
7 embodiment, prior to searching, each dimension in the MD feature space is
8 divided into a number of intervals. When a query point is received, a single
9 interval that overlaps the query point is selected from each dimension. A reduced
10 set of MD data objects is then selected that includes only those MD data objects
11 that overlap the selected intervals. This reduced set of MD data objects, rather than
12 the entire set of MD data objects in the feature space, is then used to determine
13 matches for the query point, thereby greatly increasing the efficiency of the search
14 process.

15 16 **BRIEF DESCRIPTION OF THE DRAWINGS**

17 Fig. 1 illustrates an exemplary data mapping and searching system.

18 Fig. 2 illustrates an exemplary feature space of the data mapping and
19 searching system of Fig. 1.

20 Fig. 3 is an exemplary operational flow diagram illustrating various
21 operations that may be performed in preparation for searching the feature space of
22 Fig. 2.

23 Fig. 4 is another exemplary operational flow diagram illustrating various
24 operations that may be performed in preparation for searching the feature space of
25 Fig. 2.

1 Fig. 5 is an exemplary operational flow diagram illustrating various
2 operations that may be performed in searching the feature space of Fig. 2.

3 Fig. 6 is another exemplary operational flow diagram illustrating various
4 operations that may be performed in searching the feature space of Fig. 2.

5 FIG. 7 illustrates one embodiment of a computing system in which the data
6 mapping and searching system of Fig. 1 and the operations flows of Figs. 4 - 6
7 may be implemented.

8 **DETAILED DESCRIPTION**

9 In general, the systems and methods described herein relate to, or may be
10 used in conjunction with, searching a plurality of multidimensional (MD) data
11 objects to determine which one or ones of the MD data objects overlap a given
12 query point. In accordance with various embodiments, MD data objects are
13 represented as hyper-rectangles in a feature space. If the MD data objects to be
14 searched are not hyper-rectangles, the MD data objects are first mapped to hyper-
15 rectangles in a feature space. To facilitate rapid searching of the hyper-rectangles,
16 each dimension in the feature space is first divided into a number of predetermined
17 intervals. A bit vector index is then created for each interval in each dimension.
18 Each bit vector index indicates whether each of the hyper-rectangles in the feature
19 space does or does not overlap the interval associated with the bit vector.

20 When a query point is received, a single interval that overlaps the query
21 point is selected from each dimension. The bit vector indices associated with each
22 of the selected intervals are then logically ANDed together to form a single result
23 bit vector index. The result bit vector index identifies a reduced set of hyper-
24 rectangles within the feature space. This reduced set of hyper-rectangles, or MD
25 data objects approximated by the hyper-rectangles in the reduced set, may then be

1 quickly searched using a linear scan to determine a match or matches for the query
2 point.

3 Turning now to Fig. 1, illustrated therein is one embodiment of an
4 exemplary data mapping and searching system 100. As shown, the searching
5 system 100 includes a data store 102, a mapping module 104, a search module
6 106, a shape approximator module 108, and an MD feature space 110. Included in
7 the data store 102 are a number of data items 112 (D_1 through D_n). Coupled to the
8 MD feature space 110 are a number of MD data objects of a first type 114 (S_1
9 through S_n) and a number of MD data objects of a second type 116 (R_1 through
10 R_n).

11 In accordance with one implementation, the MD feature space 110 is
12 a type that is used for mapping, manipulating, storing, and/or accessing MD data
13 points or objects in a computing system or computing process. In accordance with
14 this implementation, MD data points in the MD feature space 110 are vectors of
15 values. These vectors have length equal to the number of dimensions in the MD
16 feature space. The precise form and meaning of each index in these vectors may
17 vary, depending on the form of the MD feature space. In accordance with this
18 implementation, the MD data objects 114 and 116 are sets of MD data points. The
19 MD data objects 114 and 115 may be defined as functions or algorithms that
20 determine whether an MD data point is a member of the set of data points defined
21 by the MD object. As used herein, an MD data object is said to be "coupled to" an
22 MD feature space when the underlying function or algorithm that defines the MD
23 object manipulates vectors whose type corresponds to the MD feature space.

24 Those skilled in the art will appreciate that MD data points and objects may
25 be described or defined in terms of geometry. In accordance with this geometric

1 definition, MD data point vectors are considered coordinates in a high-
2 dimensional space. MD data objects are sets of MD data points, hence may be
3 considered to be shapes or regions in this high-dimensional space. As such, MD
4 data points or objects are referred to herein as being "in" or "within" or "coupled
5 to" an MD feature space. An MD feature space is said to "include" an MD data
6 point or object.

7 With respecting to searching in the MD feature space 112, an MD data
8 point that is subject to search is referred to herein as a query point. An MD data
9 object is said to overlap a query point if the query point is a member of the set of
10 MD data points that make up the MD data object. This set membership can be
11 determined by applying the underlying function or algorithm of the MD object to
12 the query point. Further, an MD data object is said to match the query point if the
13 MD data object is likely to overlap the query point. Matching is therefore an
14 approximation to overlap. The phrase "searching a feature space" is used herein to
15 describe performing matching and overlap operations of MD data points and
16 objects that are coupled to the MD feature space.

17 In general, the search module 106 is operable to determine which of the
18 data items 112 in the data store 102 matches a given query point 122. However, as
19 explained in detail below, the search module 106 does not search the data items
20 112 in data store 102 directly. Rather, the data items 112 are first mapped to MD
21 data objects in the feature space 110 by the mapping module 104. The search
22 module 106 then evaluates the query point and the MD data objects in the feature
23 space 110 to determine which MD data objects match the query point 122.

24 In accordance with one implementation, the mapping module 104 maps the
25 data items 112 directly to MD data objects of a second type 116. It is then with

1 respect to the MD data objects of the second type 116 that the search module 106
2 conducts the search. In accordance with another implementation, the mapping
3 module 104 maps the data items 112 to MD data objects of the first type 114. In
4 this embodiment, the shape approximator module 108 then converts or maps the
5 MD data objects of the first type 114 to MD data objects of the second type 116.
6 The search module 106 then conducts the search with respect to the MD data
7 objects of the second type 116 and/or the MD data objects of the first type 114.

8 In accordance with one embodiment, the data store 102 is composed of or
9 includes computer-readable media. For example, and without limitation, in
10 accordance with one implementation, the data store 102 is a database having data
11 objects stored on a computer-readable media, such as magnetic or optical media.
12 As used herein, computer-readable media may be any available media that can
13 store and/or embody data and/or computer executable instructions, and that may
14 be accessed by a computing system or computing process. Computer-readable
15 media may include, without limitation, both volatile and nonvolatile media,
16 removable and non-removable media, and modulated data signals. The term
17 “modulated data signal” refers to a signal that has one or more of its characteristics
18 set or changed in such a manner as to encode information in the signal.

19 In accordance with one implementation, each of the data items 112 in the
20 data store 102 is a data sample or file. For example, and without limitation, in
21 accordance with one implementation, each of the data items 112 is a media sample
22 or file, such as an audio or video sample or file. In accordance with other
23 implementations, the data items 112 may be other types of samples or files.

24 In general, the mapping module 104 is operable to map data items 112 in
25 the data store to MD data objects in the feature space 108. As previously noted,

1 the data items 112 may be mapped either as MD data objects of the first type 114
2 or as MD data objects of a second type 116. However, as described in greater
3 detail below, the mapping module 104 will typically map data items 112 to MD
4 data objects of the first type 114.

5 Those skilled in the art will appreciate that there are many different types
6 (shapes) and sizes of MD data objects. Two common types of MD data objects are
7 hyper-spheres and hyper-rectangles. Other types of MD data objects are, without
8 limitation, hyper-ellipsoids or polytopes.

9 As explained in greater detail below, in accordance with various
10 embodiments described herein, the MD data objects of a first type 114 are hyper-
11 spheres and the MD data objects of a second type 116 are hyper-rectangles. As
12 such, for simplicity, the MD data objects of the first type 114 will be referred to
13 herein as hyper-spheres and the MD data objects of the second type 116 will be
14 referred to herein as hyper-rectangles. However, it should be understood that the
15 various methods and systems described herein may be equally applicable where
16 the MD data objects of the first type are other varieties of MD data objects.

17 A hyper-rectangle may be defined as a set of all points in an MD feature
18 space such that each point has a value in each dimension in the feature space, the
19 value lying between a minimum and a maximum value per dimension. A hyper-
20 sphere may be defined as a set of all points in an MD feature space such that each
21 point has Euclidean distance to a fixed point less than or equal to a threshold. The
22 fixed point is known as the center of the hyper-sphere.

23 Turning to Fig. 2, illustrated therein is a generalized exemplary
24 representation of the feature space 110 including a number of hyper-rectangles
25 214-222. To simplify presentation, a 2-dimensional feature space including 2-

1 dimensional hyper-rectangles is shown. However, it should be understood that the
2 feature space 110, and the hyper-rectangles included therein, may have any
3 positive number of dimensions.

4 As shown in Fig. 2, the feature space 110 has a first dimension (dim1) 210
5 and a second dimension (dim2) 212. As previously noted, each dimension in a
6 feature space 110 can attain a range of possible values. This range of possible
7 values is shown along each dimension. While only positive integer values are
8 shown along the dimensions 210 and 212 in Fig. 2, it will be appreciated that each
9 dimension may also include negative values and floating point values. Likewise, it
10 should be appreciated that while only hyper-rectangles having positive integer
11 value ranges are shown in Fig. 2, hyper-rectangles that have value ranges that
12 extend into negative values, hyper-rectangles having only negative value ranges,
13 or hyper-rectangles having floating point value ranges are also possible.

14 A number of different conventions may be used in specifying the size and
15 location of the hyper-rectangles in a feature space 110. FIG 2 illustrates one
16 exemplary convention that may be used in specifying the size and location of the
17 hyper-rectangles in the feature space 110. In particular, each hyper-rectangle in the
18 feature space 110 includes an identifier (R1, R2, . . . , etc.) and two coordinate
19 pairs. As shown, the first coordinate pair identifies the location of the lower left
20 corner of the hyper-rectangle and the second coordinate pair indicates the upper
21 right corner of the hyper-rectangle with respect to the feature space 110. For
22 example, the lower left most hyper-rectangle 214 in the feature space is designated
23 as R1 {1,1} – {4,2}. In this example, R1 indicates the hyper-rectangle identifier,
24 {1,1} indicates the lower left corner of the hyper-rectangle 214, and {4,2}
25 indicates the upper right corner of the hyper-rectangle 214. As will be appreciated,

1 the ranges of the attributes of the hyper-rectangles R1 through R5 along
2 dimensions one and two may be determined from these ordered pairs.

3 Returning now to Fig. 1, in accordance with one implementation, the search
4 module 106, the mapping module 104, and the shape approximator module 108 are
5 each composed of, or include, computer executable instructions. In accordance
6 with one implementation these computer executable instructions are stored or
7 embodied in one or more types of computer-readable media and are executed by
8 one or more computing processes or devices, such as shown and described below
9 with respect to Fig. 7.

10 It should be understood that while the search module 106, the mapping
11 module 104, and the shape approximator module 108 are described herein as
12 comprising or including computer executable instructions embodied in computer-
13 readable media, the search module 106, the mapping module 104, the shape
14 approximator module 108, and any or all of the functions or operations performed
15 thereby, may likewise be embodied all or in part as interconnected machine logic
16 circuits or circuit modules within a computing device. Stated another way, it is
17 contemplated that the search module 106, the mapping module 104, the shape
18 approximator module 108, and their operations and functions, may be
19 implemented as hardware, software, firmware, or various combinations of
20 hardware, software, and/or firmware.

21 In general, as previously described, the shape approximator module 108 is
22 operable to map or convert hyper-spheres 114 to hyper-rectangles 116 in the
23 feature space 110. The manner in which this mapping is accomplished by the
24 shape approximator module 108 may vary, based on the type of hyper-sphere 114
25 that is being mapped or converted. For example, and without limitation, in

1 accordance with one implementation, each hyper-sphere 114 is mapped to a hyper-
2 rectangle 116 having a size that completely encloses the hyper-sphere 114. For
3 example, a hyper-sphere 114 may be mapped to a hyper-rectangle 116 having
4 dimensions such that if the hyper-sphere 114 were positioned in the center of the
5 hyper-rectangle 116, the hyper-sphere 114 would be completely contained within
6 the hyper-rectangle 116. As such, it will be appreciated that the overall size or
7 volume of a hyper-rectangle will be dependent on the overall size or volume of the
8 hyper-sphere from which it is mapped.

9 In one implementation, each hyper-rectangle 116 will be the smallest
10 possible hyper-rectangle that would completely enclose the hyper-sphere 114 from
11 which it is mapped. In other implementations, if false negative search results are
12 permissible, each hyper-rectangle 116 may be the smaller than the smallest
13 possible hyper-rectangle that would completely enclose the hyper-sphere 114 from
14 which it is mapped.

15 It should be understood, that while the hyper-rectangles 116 have been
16 described as being mapped from hyper-spheres in the feature space 110 using the
17 shape approximator module 108, in accordance with other embodiments, the
18 hyper-rectangles 116 in the feature space may be created in, or mapped to, the
19 feature space 110 using other modules or systems or mapping techniques.

20 In general, the search module 106 performs searches of the feature space
21 110 to identify hyper-rectangles that overlap a given query point 122. Given that a
22 hyper-rectangle is an MD data object, the definition of overlapping and matching a
23 hyper-rectangle is described, above. In accordance with one implementation, the
24 search module 106 performs the operations illustrated in FIGS. 3, 4, 5, and/or 6, as
25 will now be described.

1 Turning first to Fig. 3, illustrated therein is an exemplary operational flow
2 including operations 300 that may be performed by the search module prior to
3 searching the feature space 110. In accordance with one implementation, the
4 operations 300 are performed once the feature space 110 has been populated with
5 hyper-rectangles 116. As described in greater detail below, the operations 300
6 create a set of bit vector indices that are used during the search process. The
7 operations 300 may be performed at various times. Typically, however, the
8 operations 300 will not be performed before each search operation. Rather, the
9 operations 300 will typically be performed when a large number of hyper-
10 rectangles 116 have been added or removed from the feature space 110. For
11 example, the operations 300 may only be performed after a given number of
12 modifications have taken place with respect to the bit vector indices.

13 As shown in Fig. 3, at the start of the operational flow 300, a partition
14 operation 310 partitions each dimension in the feature space 110 into a number of
15 disjoint intervals. For example, as shown in Fig. 2, both dimensions 210 and 212
16 have both been partitioned into three disjoint intervals. As shown, dimension one
17 210 has been partitioned into interval one, which encompasses all values in
18 dimension one 210 below the value 4; interval two 226, which encompasses all
19 values in dimension one between values 4 and 8; and interval three 228, which
20 encompasses all values in dimension one above value 8. While not specifically
21 shown, dimension two, and any other dimensions in the feature space 110, would
22 be partitioned in a similar manner.

23 The precise manner in which the starting and ending points of the intervals
24 are determined may vary, and may be dependent on such things as hyper-rectangle
25 distribution and/or hyper-rectangle size. For example, and without limitation, in

1 accordance with one implementation, when m intervals are desired, $m - 1$
2 divisions or interval dividers are selected between the intervals. For example, as
3 shown in Fig. 2, three intervals require the selection of two interval dividers ($3 - 1$
4 $= 2$). In accordance with this implementation, the first and last interval in each
5 dimension will be unbounded on one side. For example, as shown in Fig. 2,
6 interval one 210 is bounded on one side by value 4, but remains unbounded at its
7 other side. Similarly, interval two 212 is bounded on one side by value 8, but
8 remains unbounded at its other side.

9 In accordance with one implementation, the position of each interval
10 divider is selected such that it falls either at the beginning or end (boundary) of a
11 value range of one of the hyper-rectangles in the feature space. For example, as
12 shown in Fig. 2, the divider 230 between interval one 224 and interval two 226
13 occurs at the end of the value range of R1 214 along dimension one 210.
14 Similarly, the divider 232 between interval two 225 and interval three 228 occurs
15 at the end of the value range of R2 216 along dimension one 210.

16 In accordance with one implementation, the locations of the interval
17 dividers are determined as follows. Assuming $|S|$ equals the number of hyper-
18 rectangles in the feature space, m is the desired number of intervals, a/b is used to
19 represent division of b into a with integer truncation, $a\%b$ represents the remainder
20 of the division a/b , and $k=(2*|S|)\%m$.

$$\text{Equation(1) } \text{FirstIDs}_j = j * [(2 * |S|) / m] + j \quad 1 \leq j \leq k$$

$$\text{Equation (2) } \text{RemainingIDs}_j = j * [(2 * |S|) / m] + k \quad k+1 \leq j \leq m$$

23 Equation (1) gives the IDs (where $ID=n$ is the n^{th} smallest hyper-rectangle
24 boundary along the axis) of the first k of the m dividers [$j=1$ to k] relative to the
25 minimum boundary ID and sorted in increasing order. Equation (2) gives the IDs

1 of the remaining dividers. For instance, if $\text{FirstIDS}_1=5$, then the first divider is at
2 the 5th smallest hyper-rectangle boundary along the axis. In this implementation,
3 the idea is to allocate approximately equal numbers of MD data objects to each
4 interval, since this ultimately results in more efficient search.

5 Using Equations (1) with respect to the feature space and hyper-rectangles
6 shown in FIG. 2, it can be seen that $k=(2*5)\%3=1$. Therefore $\text{FirstIDS}_1 =$
7 $1*[(2*5)/3] + 1 = 4$. The first division is then at the 4th rectangle boundary (where
8 the boundaries are sorted in increasing order). Using Equations (2) with respect to
9 the feature space and hyper-rectangles shown in FIG. 2, it can be seen that
10 $\text{RemainingIDS}_2 = 2*[(2*5)/3] + 1 = 7$. Therefore, the second division is at the 7th
11 rectangle boundary. Since the 4th and 7th boundaries are at 4 and 8 respectively,
12 this is where the dividers are located. In accordance with one embodiment, a
13 restricted set of rectangle boundaries is used based upon prior knowledge of query
14 point distributions. This restricted set of boundaries would then be used in a
15 manner identical to what has been described.

16 Following the partitioning operation 310, a bit vector indices construction
17 operation then constructs a bit vector index corresponding to each interval in each
18 dimension. In particular, for each interval, a bit vector index is created that
19 specifies whether or not each of the hyper-rectangles 116 in the feature space 110
20 overlaps the interval. A hyper-rectangle 116 may be said to overlap an interval in a
21 dimension if all or a part of its value range lies within the value range specified by
22 the interval. For example, with respect to Fig. 2, each of hyper-rectangles R1 214,
23 R4 220, and R5 222 overlaps interval one 224; each of hyper-rectangles R2 216,
24 R4 220, and R5 222 overlaps interval two 226; and each of hyper-rectangles R3
25 218 and R5 222 overlaps interval three 224.

1 In accordance with one embodiment, each bit vector index includes the
2 same number of bits as there are hyper-rectangles in the feature space.
3 Furthermore, each bit in the bit vector index is associated with a single one of the
4 hyper-rectangles in the feature space. In accordance with another embodiment, bit
5 vectors may include a greater number of bits than hyper-rectangles. For example,
6 in one embodiment, when a hyper-rectangle is removed from the feature space, its
7 associated bit may simply be set to "0", rather than being removed from the bit
8 vector index.

9 Each bit in a bit vector index indicates whether or not the hyper-rectangle to
10 which it is associated overlaps the interval associated with the bit vector index. For
11 example, a bit having a value of "1" might indicate that its associated hyper-
12 rectangle overlaps the interval associated with the bit vector index, and a bit
13 having a value of "0" might indicate that its associated hyper-rectangle does not
14 overlap the interval associated with the bit vector index. For example, with respect
15 to Fig. 2, a first bit vector index associated with Interval one 224 includes five bits
16 and may be written as [1 0 0 1 1], where the first bit (1) indicates that R1 overlaps
17 interval one, the second bit (0) indicates that R2 does not overlap interval one, the
18 third bit (0) indicates that R3 does not overlap interval one, the fourth bit (1)
19 indicates that R4 overlaps interval one, and the fifth bit (1) indicates that R5
20 overlaps interval one. Using this convention, the bit vector index associated with
21 interval two 226 is [0 1 0 1 1], and the bit vector index associated with interval
22 three 228 is [0 0 1 0 1].

23 Turning now to Fig. 4, illustrated therein is a detailed exemplary
24 operational flow 400 including operations that may be used for constructing bit
25 vector indices for the feature space 110. It will be appreciated that the operational

1 flow 400 is operable to handle the construction of bit vector indices for any
2 number of dimensions in the feature space 110 and any number of dimension
3 intervals.

4 As shown, at the start of the operation flow 400, a dimension set operation
5 410 sets or initializes a dimension variable (dim) to a value of 1. Following the
6 dimension set operation 410, a partition dimension operation 412 partitions the
7 dimension "dimension(dim)" into intervals, as described above. As will be
8 appreciated, since the dimension variable dim is currently set to 1, the partition
9 dimension operation 412 will partition the first dimension of the given feature
10 space. Following the partition dimension operation 412, a set interval operation
11 414 sets or initializes an interval variable intvl to a value of 1. Next, a set hyper-
12 rectangle operation 416 sets or initializes a hyper-rectangle variable rect to a value
13 of 1.

14 Following the set hyper-rectangle operation 416, a set bit operation 418
15 determines if the hyper-rectangle specified by the hyper-rectangle variable rect
16 overlaps the interval specified by the interval variable intvl, in the dimension
17 specified by the dimension variable dim. If it is determined that the specified
18 hyper-rectangle overlaps the specified interval in the specified dimension, the set
19 bit operation 418 sets a bit associated with the specified hyper-rectangle in a bit
20 vector index associated with the specified interval in the specified dimension to 1.
21 If, however, it is determined that the specified hyper-rectangle does not overlap
22 the specified interval in the specified dimension, the set bit operation 418 sets a bit
23 associated with the specified hyper-rectangle in a bit vector index associated with
24 the specified interval in the specified dimension to 0.

1 Next, an increment hyper-rectangle operation 420 increments the hyper-
2 rectangle variable rect. A rectangle number determination operation 422 then
3 determines if the hyper-rectangle variable rect is equal to the number of hyper-
4 rectangles in the feature space plus 1. If the hyper-rectangle variable rect is not
5 equal to the number of hyper-rectangles in the feature space, the operational flow
6 400 returns to the set bit operation 418. However, if the hyper-rectangle variable
7 rect is equal to the number of hyper-rectangles in the feature space plus 1, the
8 operational flow 400 proceeds to an increment interval operation 424, where the
9 interval variable intvl is incremented.

10 Following the increment interval operation 424, an interval determination
11 operation 426 determines if the interval variable intvl equals the number of
12 intervals in the dimension specified by dimension variable dim plus 1. If the
13 interval variable intvl does not equal the number of intervals in the dimension
14 specified by dimension variable dim plus 1, the operational flow returns to the set
15 hyper-rectangle operation 416. However, if the interval variable intvl does equal
16 the number of intervals in the dimension specified by dimension variable dim plus
17 1, the operational flow proceeds to an increment dimension operation 428, where
18 the dimension variable dim is incremented.

19 Following the increment dimension operation 428, a dimension
20 determination operation 430 determines if the dimension variable dim equals the
21 number of dimensions in the feature space plus 1. If the dimension variable dim
22 does not equal the number of dimensions in the feature space plus 1, the
23 operational flow 400 returns to the partition dimension operation 412. However, if
24 the dimension variable dim does equal the number of dimensions in the feature
25 space plus 1, the operational flow 400 ends.

1 Turning now to Fig. 5, illustrated therein is an exemplary operational flow
2 500 that may be used in searching the feature space 110. More particularly, the
3 operational flow 500 may be used in searching the feature space 110 after bit
4 vector indices have been created for each of the intervals in the feature space 110,
5 either in accordance with the operational flows 300 and/or 400, as described
6 above, or by some other operations. As shown, at the beginning of the operational
7 flow 500, a receive query operation 514 receives a query item. Next, a map query
8 operation 515 maps that query item into a query point in the MD feature space.

9 Following the map query operation 515, and interval selection operation
10 516 selects an interval from each dimension that overlaps the query point. An
11 interval in a dimension may be said to overlap a query point if the value of the
12 query point in the dimension lies within the value range specified by the interval.
13 Next, an ANDing operation 518 logically ANDs all of the bit vector indices
14 corresponding to the intervals selected in the interval selection operation 516. This
15 logical ANDing of the bit vector indices produces a single result bit vector index
16 that specifies a set of hyper-rectangles that match the received query point. As will
17 be appreciated, the set of hyper-rectangles specified by the result bit vector index
18 will in most cases be significantly smaller than the set of all hyper-rectangles
19 within the feature space 110.

20 Following the ANDing operation 518, a matching operation 520 compares
21 the received query point to each of the hyper-rectangles indexed by 1s in the result
22 bit vector index to determine which of these hyper-rectangles overlap the received
23 query point. In the case where each of the hyper-rectangles is mapped from an
24 associated MD data object, rather than comparing the received query point to each
25 of the hyper-rectangles specified by the result bit vector index, the received query

1 point may be compared directly to the MD data object associated with the hyper-
2 rectangles indexed by 1s in the result bit vector index.

3 Turning now to Fig. 6, illustrated therein is another, more detailed
4 exemplary operational flow 600 including operations that may be used for
5 searching a feature space 110. As with the operational flow, the operational flow
6 600 may be carried out after bit vector indices have been created for each of the
7 intervals in the feature space 110, whether in accordance with the operational
8 flows 300 and/or 400, as described above, or by some other operations. As shown,
9 at the beginning of the operational flow 600, a receive query operation 610
10 receives a query point. After a query point has been received, a set dimension
11 operation 612 sets a dimension variable dim equal to 1. Next, a determine interval
12 operation 614 determines an interval in the dimension specified by the dimension
13 variable dim that includes the query point. Stated another way, interval operation
14 614 determines an interval in the dimension specified by the dimension variable
15 dim that overlaps the query point. A select bit vector index operation 616 then
16 selects the bit vector index corresponding to the interval determined in determine
17 interval operation 614.

18 Following the select bit vector index operation 616, a dimension
19 determination operation 618 determines if the dimension variable dim is equal to
20 1. If the dimension dim is equal to 1, a set result bit vector index operation 620
21 sets the result bit vector index equal to the bit vector index selected in the select bit
22 vector index operation 616, and the operational flow proceeds to a dimension
23 variable increment operation 624. However, if the dimension determination
24 operation 618 determines that the dimension variable dim is not equal to 1, the
25 operational flow 600 proceeds to an ANDing operation 622, where the bit vector

1 index selected in the select bit vector index operation 616 is logically ANDed
2 with, or into, the result bit vector. Next, the dimension variable increment
3 operation 624 increments the dimension variable dim.

4 Following the dimension variable increment operation 624, a dimension
5 determination operation 626 determines if the dimension variable dim equals the
6 number of dimensions in the feature space. If the dimension variable dim does not
7 equal the number of dimensions in the feature space, the operational flow 600
8 returns to the determined interval operation 614. However, if the dimension
9 variable dim does equal the number of dimensions in the feature space, the
10 operational flow proceeds to a find hyper-rectangle operation 628, where the
11 hyper-rectangles corresponding to each "1" in the result bit vector are found. Next,
12 a compare data object operation 630 compares the received query point to all of
13 the MD data objects associated with the hyper-rectangles found by the fine hyper-
14 rectangle operation 628. A return data object operation 630 then returns all MD
15 data objects that match the received query point, and the operational flow 600
16 ends.

17 Fig. 7 illustrates one operating environment 710 in which the various
18 systems, methods, and data structures described herein may be implemented. The
19 exemplary operating environment 710 of Fig. 7 includes a general purpose
20 computing device in the form of a computer 720, including a processing unit 721,
21 a system memory 722, and a system bus 723 that operatively couples various
22 system components include the system memory to the processing unit 721. There
23 may be only one or there may be more than one processing unit 721, such that the
24 processor of computer 720 comprises a single central-processing unit (CPU), or a
25 plurality of processing units, commonly referred to as a parallel processing

1 environment. The computer 720 may be a conventional computer, a distributed
2 computer, or any other type of computer.

3 The system bus 723 may be any of several types of bus structures including
4 a memory bus or memory controller, a peripheral bus, and a local bus using any of
5 a variety of bus architectures. The system memory may also be referred to as
6 simply the memory, and includes read only memory (ROM) 724 and random
7 access memory (RAM) 725. A basic input/output system (BIOS) 726, containing
8 the basic routines that help to transfer information between elements within the
9 computer 720, such as during start-up, is stored in ROM 724. The computer 720
10 further includes a hard disk drive 727 for reading from and writing to a hard disk,
11 not shown, a magnetic disk drive 728 for reading from or writing to a removable
12 magnetic disk 729, and an optical disk drive 730 for reading from or writing to a
13 removable optical disk 731 such as a CD ROM or other optical media.

14 The hard disk drive 727, magnetic disk drive 728, and optical disk drive
15 730 are connected to the system bus 723 by a hard disk drive interface 732, a
16 magnetic disk drive interface 733, and an optical disk drive interface 734,
17 respectively. The drives and their associated computer-readable media provide
18 nonvolatile storage of computer-readable instructions, data structures, program
19 modules and other data for the computer 720. It should be appreciated by those
20 skilled in the art that any type of computer-readable media which can store data
21 that is accessible by a computer, such as magnetic cassettes, flash memory cards,
22 digital video disks, Bernoulli cartridges, random access memories (RAMs), read
23 only memories (ROMs), and the like, may be used in the exemplary operating
24 environment.

1 A number of program modules may be stored on the hard disk, magnetic
2 disk 729, optical disk 731, ROM 724, or RAM 725, including an operating system
3 735, one or more application programs 736, other program modules 737, and
4 program data 738. A user may enter commands and information into the personal
5 computer 720 through input devices such as a keyboard 40 and pointing device
6 742. Other input devices (not shown) may include a microphone, joystick, game
7 pad, satellite dish, scanner, or the like. These and other input devices are often
8 connected to the processing unit 721 through a serial port interface 746 that is
9 coupled to the system bus, but may be connected by other interfaces, such as a
10 parallel port, game port, or a universal serial bus (USB). A monitor 747 or other
11 type of display device is also connected to the system bus 723 via an interface,
12 such as a video adapter 748. In addition to the monitor, computers typically
13 include other peripheral output devices (not shown), such as speakers and printers.

14 The computer 720 may operate in a networked environment using logical
15 connections to one or more remote computers, such as remote computer 749.
16 These logical connections may be achieved by a communication device coupled to
17 or a part of the computer 720, or in other manners. The remote computer 749 may
18 be another computer, a server, a router, a network PC, a client, a peer device or
19 other common network node, and typically includes many or all of the elements
20 described above relative to the computer 720, although only a memory storage
21 device 750 has been illustrated in Fig. 7. The logical connections depicted in Fig.
22 7 include a local-area network (LAN) 751 and a wide-area network (WAN) 752.
23 Such networking environments are commonplace in office networks, enterprise-
24 wide computer networks, intranets and the Internet, which are all types of
25 networks.

1 When used in a LAN-networking environment, the computer 720 is
2 connected to the local network 751 through a network interface or adapter 753,
3 which is one type of communications device. When used in a WAN-networking
4 environment, the computer 720 typically includes a modem 754, a type of
5 communications device, or any other type of communications device for
6 establishing communications over the wide area network 752. The modem 754,
7 which may be internal or external, is connected to the system bus 723 via the serial
8 port interface 746. In a networked environment, program modules depicted
9 relative to the personal computer 720, or portions thereof, may be stored in the
10 remote memory storage device. It is appreciated that the network connections
11 shown are exemplary and other means of and communications devices for
12 establishing a communications link between the computers may be used.

13 Various systems and methods have been set forth that may be used in, or in
14 conjunction with various searching methods using hyper-rectangles and bit vector
15 indices. The systems, methods, and data structures have been described as
16 incorporating various elements or operations recited in the appended claims. It
17 should be understood, however, that the preceding description is not intended to
18 limit the scope of this patent. Rather, the inventors have contemplated that the
19 claimed systems, methods, and data structures might also be embodied in other
20 ways, to include different operations or elements, or combinations of operations or
21 elements, similar to the ones described, in conjunction with other present or future
22 technologies.